

## Communication

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*Nano Lett.*, **Just Accepted Manuscript** • DOI: 10.1021/acs.nanolett.5b05161 • Publication Date (Web): 07 Mar 2016

Downloaded from <http://pubs.acs.org> on March 7, 2016

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## Hofstadter Butterfly and Many body effects in epitaxial graphene superlattice

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**Abstract:** Graphene placed on h-BN has received a wide range of interests due to the improved electrical performance and rich physics from the interface, especially the emergence of superlattice Dirac points as well as Hofstadter butterfly in high magnetic field. Instead of transferring graphene onto h-BN, epitaxial growth of graphene directly on a single-crystal h-BN provides an alternative and promising way to study these interesting superlattice effects due to their precise lattice alignment. Here we report an electrical transport study on epitaxial graphene superlattice on h-BN with a period of  $\sim 15.6$  nm. The epitaxial graphene superlattice is clean, intrinsic, and of high quality with a carrier mobility of  $\sim 27,000$   $\text{cm}^2\text{V}^{-1}\text{s}^{-1}$ , enabling to observe Hofstadter butterfly features originated from the superlattice at a magnetic field as low as 6.4 T. A metal-insulator transition and magnetic field dependent Fermi velocity were also observed, suggesting prominent electron-electron interaction-induced many body effects.

**Key words:** Graphene superlattice, Hofstadter butterfly, Metal-insulator transition, Fermi velocity, Many body effect

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3 Due to the 2D nature of graphene<sup>1, 2</sup>, interfaces play an important role in  
4 modulation of graphene's electronic properties. By placing graphene on top of  
5 hexagonal boron nitride (h-BN), a rather clean and flat interface could be achieved,  
6 leading to a suppressed charge inhomogeneity and an enhanced mobility<sup>3, 4</sup>. Such  
7 clean interfaces would introduce strong electron-electron (e-e) interaction, causing  
8 metal insulator transition (MIT)<sup>5, 6</sup>, quantum Hall ferromagnetism (QHFM)<sup>7-9</sup> and  
9 Fermi velocity renormalization in graphene<sup>10-12</sup>. When the relative lattice rotation  
10 angle between graphene and h-BN approaches zero, the lattice mismatch induced  
11 moiré pattern has the largest period, i.e.  $\lambda \sim 15\text{nm}$ <sup>13</sup>. This moiré pattern is more than a  
12 geometrical superstructure, and it brings a periodic potential modulation to the  
13 original graphene lattice and reshapes the band structure of graphene by producing  
14 superlattice minibands<sup>13-19</sup>. The quantum Hall effect (QHE) in such moiré superlattice  
15 has a phase diagram with a fractal structure, so called Hofstadter butterfly<sup>17-24</sup>. It has  
16 been experimentally observed that the magnetic minibands repeat in a self-similar  
17 way at rational values  $\Phi/\Phi_0 = p/q$ , where  $\Phi$  is the magnetic flux through the  
18 superlattice unit cell,  $\Phi_0 = h/e$  is the magnetic flux quantum, and  $p, q$  are integers<sup>17-19</sup>.  
19 The description of the fractal spectra involves the introduction of Diophantine relation  
20  $n/n_0 = t(\Phi/\Phi_0) + s$ , where  $t$  and  $s$  are integers referred to superlattice minibands index<sup>17</sup>,  
21 <sup>18</sup>, with  $n_0 = 1/A$ ,  $A = \sqrt{3}\lambda^2/2$  the area of superlattice unit cell, and  $n$  the carrier density.  
22 Usually, the experimental access to Hofstadter butterfly spectrum is difficult, thus a  
23 clean interface between graphene and h-BN with a nearly zero lattice rotation angle is  
24 highly desired to study the Hofstadter butterfly features at low magnetic fields.  
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40 In this paper, we present the magneto-transport measurements of the precisely  
41 aligned graphene on h-BN (G/h-BN). The zero-twisted G/h-BN samples with clean  
42 and intrinsic interfaces were prepared by Van der Waals epitaxial growth technique<sup>13</sup>.  
43 We identified typically two kinds of Hofstadter butterfly gaps aside from the single  
44 particle gap<sup>25, 26</sup> and the many body QFHM gap<sup>7, 8</sup> with Landau levels (LLs) from the  
45 main Dirac point (DP). The first ones are fanned out from the superlattice Dirac  
46 points (SDPs), similar to LLs fanned out from the DP, and they are Hofstadter  
47 minibands in the regime of strong superlattice modulation<sup>22</sup>. While the second ones  
48 are the gaps generated from the intersections of LLs from DP and SDPs and are  
49 attributed to LLs originating from replica Dirac spectra quantized in the effective  
50 magnetic field,  $B_{\text{eff}}^{17-19, 22}$ . Here,  $B_{\text{eff}} = \pm |B - B_{1/q}|$  with  $q = 3$  and  $4$ , which correspond to a  
51 magnetic field of 6.4 T and 4.8 T, respectively. Note that both single particle and  
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3 many body gaps contribute to the observed Hofstadter minibands, suggesting strong  
4 e-e interactions in our epitaxial G/h-BN samples. More experimental evidences of e-e  
5 interactions are provided in a metal insulator transition (MIT) over a wide range of  
6 carrier density at a temperature of around 30K, as well as a magnetic field dependent  
7 Fermi velocity.  
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11 Figure 1a shows a Hall bar device fabricated from the epitaxial G/h-BN. The  
12 thickness of h-BN flake (exfoliated on 300nm SiO<sub>2</sub>/(p++)Si substrate) is ~70 nm.  
13 Monolayer graphene was epitaxially grown on h-BN by a low temperature plasma-  
14 enhanced chemical vapor deposition (PECVD) technique<sup>13</sup>. The as-grown graphene is  
15 single crystalline and its lattice rotation relative to the underneath h-BN is zero. Moiré  
16 superlattice with a period of ~15.6 nm is shown in the atomic force microscopy  
17 (AFM) height image (Fig. 1b). Standard electron beam lithography, contact metal  
18 deposition (100nm-Au/2nm-Ti) and lift-off techniques were utilized for device  
19 fabrications. Note that no reactive ion etching (RIE) was applied during the device  
20 fabrication process in order to avoid any possible structural damages or external  
21 contaminations to the device. Fig. 1c shows a typical transfer curve of the device at  
22  $T=1.8\text{K}$ . Dirac point locates at  $V_g=-0.4\text{V}$ , indicating negligible doping; and it shows a  
23 very narrow resistance peak with an estimated electron mobility of  $\sim 27,000\text{ cm}^2\text{V}^{-1}\text{s}^{-1}$ ,  
24 which is about 5 times higher than that of our previously reported device in ref.13  
25 with a RIE process. The SDPs can be seen at both electron and hole side (Fig. 1c) as  
26 two satellite resistance peaks beside the main Dirac point with  $\Delta V_g \sim 36\text{ V}$ . Similar to  
27 the previous findings<sup>13, 16-19</sup>, these two resistance peaks are strongly asymmetric.  
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31 Figure 2a depicts a quantum Hall fan diagram with a color mapping of  $R_{xx}$  with  
32 respect to the gate voltages and magnetic fields at a temperature of  $T=1.8\text{K}$ . LLs from  
33 Dirac fermions can be clearly identified as the resistance minima fanning out from  
34 DP, including both normal quantum Hall (QH) states ( $\nu = 4n+2$ , where  $n=0, \pm 1, \pm 2 \dots$   
35 is LL index) and symmetry broken QH states ( $\nu = 0, \pm 1$ , and  $4n$ ). A line cut of Fig. 2a  
36 at  $B \sim 9\text{T}$  is shown in Fig. 2b and a lift of LLs degeneracy is clearly demonstrated in  
37 the inset of Fig. 2b as symmetry broken states develops at  $\nu=0, \pm 1$ , and  $\nu = 4n$   
38 at higher carrier densities. Particularly, the onset of  $\nu=1$  state starts as low as 3T  
39 (Supplementary Fig. S2). The emergence of these symmetry broken states at such a  
40 low magnetic field is due to two possible reasons: the moiré potential induced  
41 breaking of sublattice symmetry<sup>18</sup> and the e-e interaction induced many body QHFM  
42 gaps<sup>7, 22, 27, 28</sup>. Note that a breaking of sublattice symmetry would also induce an  
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3 energy gap at main DP<sup>18</sup>; however we didn't see any obvious gap features in our  
4 transport data, indicating this factor makes little contribution. On the other hand, the  
5 e-e interactions are estimated to be more pronounced owing to the clean and intrinsic  
6 interface between graphene and hBN. Thus, we attribute the observed symmetry  
7 broken states mainly from the nontrivial e-e interaction induced QHFM gaps.  
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11 It is also worth noting that a mapping of  $R_{xx}$  alone is not sufficient to identify  
12 Hofstadter butterfly states; thus, we take Hall resistance into account and plot a color  
13 mapping of longitudinal conductance  $\sigma_{xx} = R_{xx}/(R_{xx}^2 + R_{xy}^2)$  and Hall conductance  $\sigma_{xy} =$   
14  $R_{xy}/(R_{xx}^2 + R_{xy}^2)$ . Figure 3a and 3b are the resulted mappings of  $\sigma_{xx}$  and  $\sigma_{xy}$  respectively,  
15 with the color contrast chosen to favor superlattice related QH states. The QH states  
16 are characterized by those  $\sigma_{xx}$  minima and  $\sigma_{xy}$  plateaus.  
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21 From these mappings, we can see that there are typically two kinds of Hofstadter  
22 butterfly gaps. The first ones are LLs like gaps fanned out from the SDPs, similar to  
23 gaps fanned out from the DP, and they are called Hofstadter minibands in the regime  
24 of strong superlattice modulation<sup>22, 23</sup>. These gaps are indicated by the white dashed  
25 lines in left panel of Fig. 3c, e.g. gaps from the SDP with  $\nu_s = 0, \pm 2$  are clearly  
26 depicted as three trenches of  $\sigma_{xx}$  minima. The second ones are the gaps that can't be  
27 traced back to either the DP or the SDPs, and they can be described as Landau levels  
28 originating from replica Dirac spectra that are quantized in effective magnetic field  
29  $B_{eff} = \pm |B - B_{1/q}|$ <sup>17-19, 22</sup>. These Hofstadter gaps are clearly revealed at  $B = B_{1/3} = 6.4$ T,  
30 where new gaps are generated at the intersection of LLs from the DP and that from  
31 the SDP. For example, the intersection of  $\nu = -10$  (grey dashed line) and  $\nu_s = 2$  (white  
32 dashed line) is shown in Fig. 3c. However, a small deviation can be found between  
33 the fractal Hofstadter bands and the LLs from the DP at  $\nu = -16$  and the SDP at  $\nu_s = -4$ ,  
34 indicated by black arrow in Fig. 3c. The deviation might be caused by the influence of  
35 a higher order superlattice effect outside of the first mini-Brillouin zone, a second  
36 generation of SDP (SSDP) as indicated in Figure S7. As a result, the spectra would be  
37 more complicated since DP, SDP, and SSDP are not equally spaced (the ratio of their  
38 spacing is  $1: (\sqrt{3}-1)$ ).  
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51 Details of the gaps are summarized in the Wannier diagram<sup>29</sup> as shown in Fig. 3d,  
52 where normalized density  $n/n_0$  is used as X-axis. The main DP is situated at  $n/n_0 = 0$ ,  
53 from which LLs are fanned out as the black (single particle gaps) and the blue (many  
54 body gaps) lines. The SDPs are located at  $n/n_0 = \pm 4$ , and similarly from which LLs  
55 like Hofstadter minibands in the regime of strong superlattice modulation are  
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3 developed including symmetry conserved (green lines) and symmetry broken (pink  
4 lines) gaps. The fractal Hofstadter spectra that experienced in a reduced effective  
5 magnetic field  $B_{eff} = \pm|B - B_{1/q}|$  are labeled as red lines with  $q=1/3$  and  $q=1/4$ . The  
6 distribution of gaps in Fig. 3d agrees with the theory<sup>23</sup> in that, for  $\Phi/\Phi_0 < 1/5$ , all the  
7 gaps can be traced back to analytically LLs of DP or SDPs. The fractal Hofstadter  
8 butterfly spectra show up until  $\Phi/\Phi_0 > 1/5$ . Besides, the gaps observed in our epitaxial  
9 G/hBN samples display quite strong thermal stability; fractal gaps at  $\Phi/\Phi_0 = 1/3$  can  
10 stay visible at  $T=30\text{K}$  (see Supplementary Figure S2) while the gaps at  $\nu_s = \pm 2$  from  
11 SDP at hole side are very stable up to  $T > 40\text{K}$ .  
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18 The observation of Hofstadter butterfly spectra at such low magnetic field can be  
19 attributed to the combination of: 1) a strong superlattice modulation; 2) a strong e-e  
20 interaction<sup>30</sup>; and 3) a reduction of extra carrier scattering from substrate due to ultra  
21 clean interface. The strong superlattice modulation is evidenced by the LLs fanning  
22 out from SDP; while the strong e-e interaction is demonstrated in those symmetry  
23 broken states originated from both DP and SDP. In fact, the strong e-e interactions are  
24 also manifested in observation of MIT and magnetic field dependent Fermi velocity.  
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30 Figure 4a shows a mapping of  $R_{xx}(T)/R_{xx}(T=1.8\text{K})$  at various carrier densities. At  
31 around DP and SDP as well within a gate modulation range of 4V, it behaves like  
32 insulator as the resistances increase all the way up as T drops down (inset of Fig. 4b),  
33 which agrees well with the literatures<sup>3</sup>. However, away from these regions, the  
34 resistances first decrease and then increase after T drops down to a critical point,  
35 suggesting a metal-insulator transition (MIT)<sup>5</sup>. The transition temperature is usually  
36 from 10K to 30K depending on the position of Fermi level. The trend is that the closer  
37 to charge neutrality points (DP or SDP) the higher the transition temperature. Similar  
38 to the literature<sup>6</sup>, the MIT in graphene occurs with decreasing rather than increasing  
39 the charge inhomogeneity. However, our results are different from the literature in two  
40 aspects. Firstly, there is no screening layer in our device; instead, we utilized the  
41 epitaxial G/h-BN with an intrinsic interface in this study. Secondly, the MIT observed  
42 in our device occurs over a wide range of charge carrier densities. The observations  
43 can be attributed to the onset of quantum interference<sup>31, 32</sup> and the superlattice  
44 modulation. The former makes electrons constrained or localized<sup>33-35</sup>, leading to the  
45 observed transition within a wide range of carrier densities at low temperature. While  
46 the latter produces extra charge neutral points (i.e. SDPs) close to the DP as well as a  
47 density of state discontinuity in between, so called Van Hove singularities<sup>16, 36, 37</sup>,  
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3 which in turn modulate the specific conducting behaviors of electrons and contribute  
4 to the sharp and prominent MIT close to these charge neutral points.

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6 Figure 5a plots Shubnikov–de Haas oscillations (SdHOs) versus magnetic fields  
7 at  $V_g=20\text{V}$  for temperature from 1.8 K to 80 K, where  $v_F$  is extracted from  
8 temperature dependent amplitudes<sup>25</sup> as shown in the inset for  $B=3\text{T}$  (corresponding to  
9  $\nu=14$ ). The result is displayed as blue stars in Fig. 5b that  $v_F$  is decreased from  
10  $1.36\times 10^6$  m/s to  $0.86\times 10^6$  m/s as magnetic field is increased from 2.3 T to 7 T. Note  
11 that we limit the gate voltage  $|V_g|=20\text{V}$  to minimize the influence from superlattice.  
12 Such a magnetic field dependent Fermi velocity is beyond the scope of single particle  
13 picture, and it indicates strong many body interactions<sup>10-12</sup>. The finding also agrees  
14 well with magneto-optical LL transitions<sup>38,39</sup>.

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16 In conclusion, we studied the transport properties of graphene superlattice  
17 obtained from epitaxial growth. The clean interface between graphene and h-BN  
18 allows us to reveal a nice picture of fractal gaps of Hofstadter butterfly developed  
19 with the filling of magnetic flux in a unit superlattice cell at a magnetic field as low as  
20 6.4 T (corresponding to a filling of 1/3 quantum flux), which has not been explored in  
21 literature<sup>17-19,22</sup>. Such intrinsic interface also gives a clue of strong e-e interactions, as  
22 evidenced by the observed MIT over a wide range of carrier densities and a  
23 renormalization of Fermi velocity to the magnetic field. Therefore, our results indicate  
24 an important role of the interface in 2D atomic crystal heterostructure on their  
25 electronic properties.

## 36 37 38 39 **Methods**

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41 **Epitaxial growth of graphene on h-BN.** h-BN flakes were prepared by mechanical  
42 exfoliation of h-BN crystals onto 300-nm  $\text{SiO}_2/\text{Si}$  substrate by Scotch tape. And then  
43 graphene was epitaxially grown on top of hBN in PECVD with a low temperature of  
44  $\sim 500$  °C as described in ref.13. The resulting graphene superlattice structure was  
45 characterized by AFM (MultiMode IIIId, Veeco Instruments Inc.) using tapping mode  
46 under ambient condition.

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48 **Devices fabrication and electric measurements for G/h-BN.** As-grown G/h-BN  
49 samples were first spin-coated with Polymethylmethacrylate (PMMA) photoresist,  
50 followed by electron beam lithography (EBL) to define electrodes. Reactive ion  
51 etching process of graphene was avoided by putting contacts at the edge of G/h-BN in  
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Hall bar geometry. Devices were then fabricated with contact metal (100nm-Au/2nm-Ti) deposition via electron beam evaporation and following standard metal lift-off technique. Transport and magnetotransport measurements were carried out in cryogenic Dewar (Janis) using standard lock-in technique (Stanford).

### Acknowledgements

G.Z. acknowledges supports of the National Basic Research Program of China (973 Program) under the grant No. 2013CB934500 and 2012CB921302, the National Science Foundation of China (NSFC) under the grant No. 91223204. Y.Z. acknowledges supports of 973 Program of China under the grant No. 2011CB921802 and NSF of China under the grant No. 11034001.

### Supporting Information

The Supporting Information provides thermal stability of QH states, onset of  $\nu = 0, 1$  at a low magnetic field, conductance at  $\Phi = \Phi_{1/3}$ , influence of quantum capacitance, weak localization effects, Fermi velocity measurements, and observation of a second generation of superlattice Dirac points.

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### Author Contributions

G.Z. and W.Y. designed the research; W.Y. performed the growth, structural characterization, device fabrication, and electrical transport measurements; X.L. helped on graphene growth; G.C provided the h-BN substrates; K.W. and T.T. synthesized h-BN crystals. W.Y., G.Z. analysed data and wrote the manuscript, and all authors discussed and commented on the paper.

### Notes

The authors declare no competing financial interests.

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### Figure legends

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43 **Figure 1| Graphene superlattice.** **a**, Optical microscopy image of the device. **b**,  
44 AFM height image of graphene superlattice structure. **c**, Transfer curve at a  
45 temperature  $T = 1.8$  K, showing superlattice Dirac points at both electron and hole  
46 sides. The scale bars in **a**, **b** are  $20 \mu\text{m}$  and  $100 \text{ nm}$  respectively.

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51 **Figure 2| Quantum Hall States in graphene superlattice.** **a**, Landau fan diagram of  
52  $R_{xx}$  as a function of back gate  $V_g$  and magnetic field  $B$  at  $T = 1.8\text{K}$ . The white dashed  
53 lines are guide eye for Landau levels (LLs) with  $\nu = 2$ . **b**, Longitudinal ( $R_{xx}$ , Pink) and  
54 Hall resistance ( $R_{xy}$ , blue) versus gate voltage  $V_g$  at  $T = 1.8 \text{ K}$ ,  $B = 9 \text{ T}$ , and the inset is  
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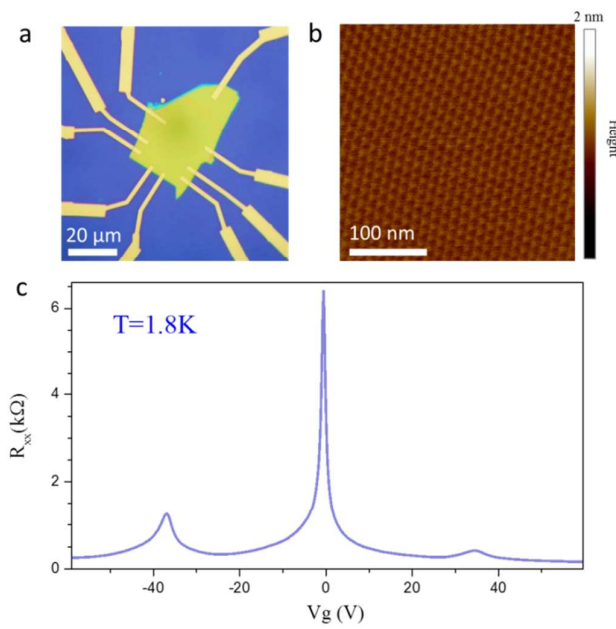
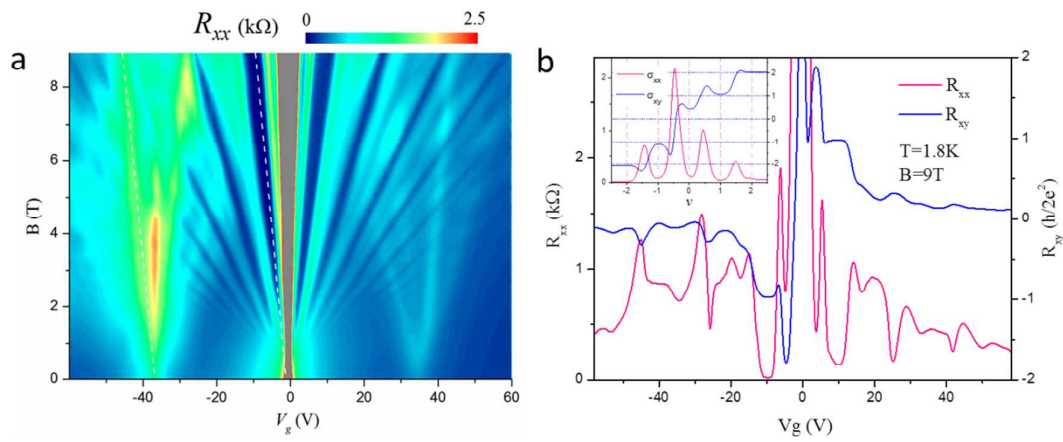
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3 the corresponding conductivity around Dirac point (DP).  
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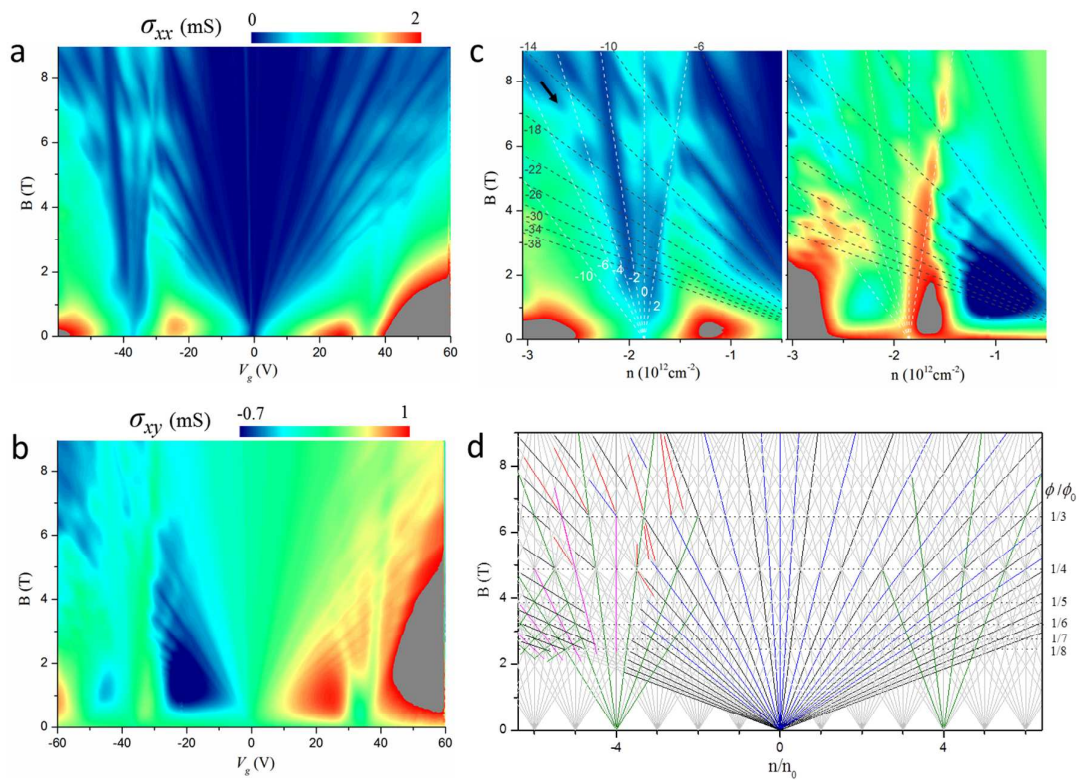
6 **Figure 3| Hofstadter butterfly spectra. a-b**, Landau fan diagram of longitudinal  
7 conductivity  $\sigma_{xx}$  (**a**) and Hall conductivity  $\sigma_{xy}$  (**b**) as a function of  $V_g$  and magnetic  
8 field  $B$  at  $T = 1.8\text{K}$ . **c** shows zoomed in images of **a** (left) and **b** (right), with the  
9 dashes lines indicating LLs from DP (grey) and SDP (white) respectively. **d**, Observed  
10 Hofstadter butterfly spectra in Wannier diagram. The assignment of colors is as  
11 followed: black and blue lines indicate single-particle and many-body gaps (due to  
12 QHFM) from main DP respectively; green (no broken symmetry) and pink (broken  
13 symmetry) lines indicate Hofstadter gaps in the regime of strong superlattice  
14 influence; red lines indicate fractal gaps originated from replica Dirac spectra that are  
15 quantized in effective magnetic field  $B_{eff} = \pm |B - B_{1/q}|$ , and here  $q = 3, 4$ .  
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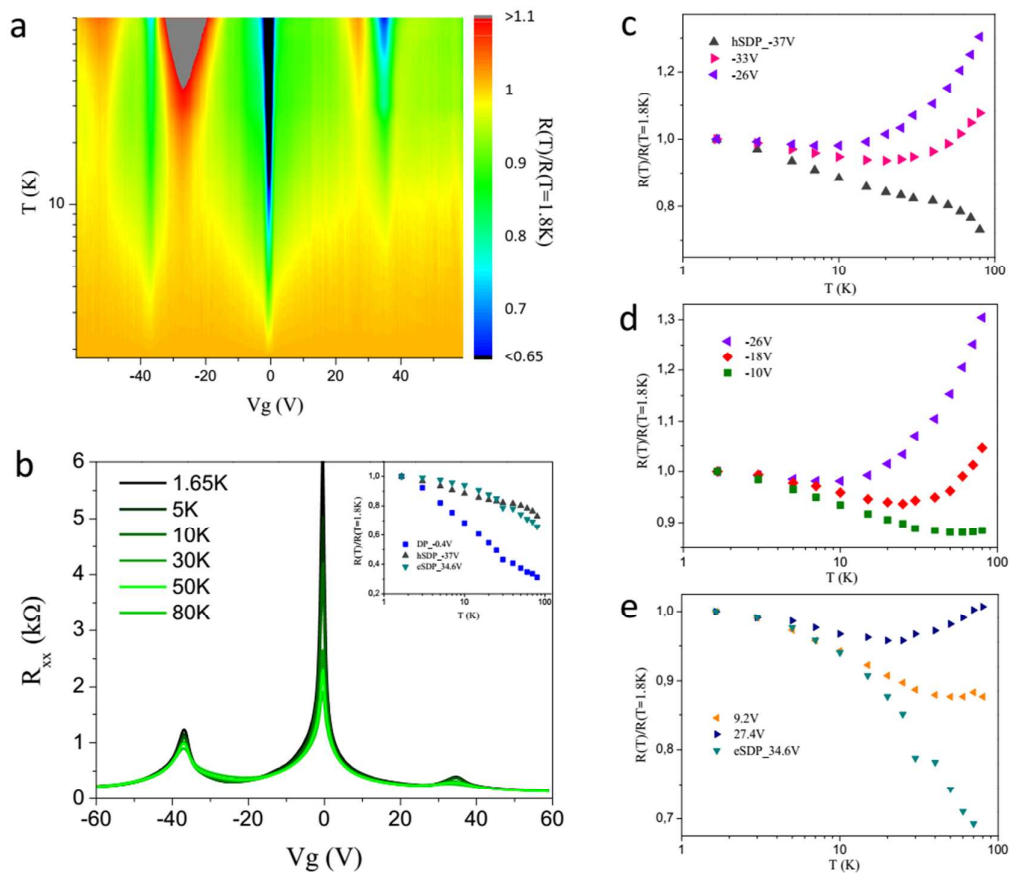
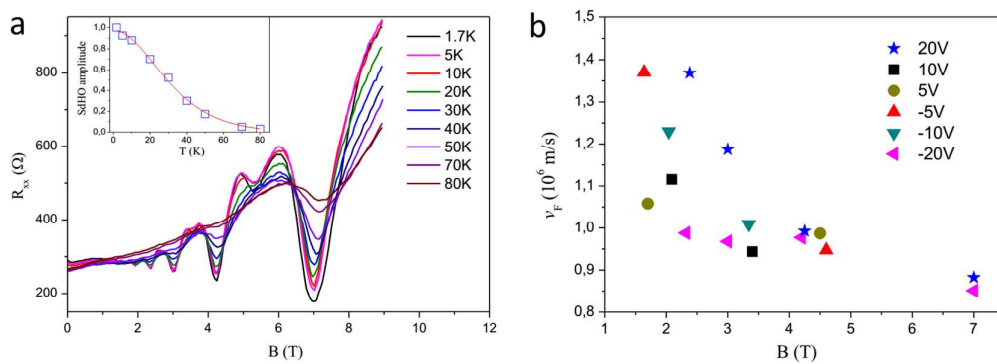
24 **Figure 4| Metal insulator transition. a**, Colored mapping of  $R(T)/R(T=1.8\text{K})$  as a  
25 function of  $V_g$  (-60 to 60 V) and  $T$  (1.65 K-80 K). **b**,  $R_{xx}$  versus  $V_g$  for different  $T$ , and  
26 the inset is the temperature dependence of resistance at DP and SDPs. **c-e** are plots of  
27  $R(T)/R(T=1.8\text{K})$  over a wide range of carrier density, revealing a transition of metal to  
28 insulating behaviors away from charge neutral points (DP and SDPs).  
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34 **Figure 5| Renormalization of Fermi velocity. a**, Shubnikov–de Haas oscillations  
35 (SdHOs) with  $R_{xx}$  versus magnetic field  $B$  (0 to 9T) at  $V_g = -20\text{ V}$  for different  $T$ , and  
36 the inset displays the T-dependent SdH amplitude at  $B = 3\text{T}$ . **b**, Plot of Fermi velocity  
37 ( $v_F$ ) as a function of  $B$  for different carrier density.  
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## Figures

Figure 1 by W. Yang, *et al.*Figure 2 by W. Yang, *et al.*

Figure 3 by W. Yang, *et al.*

Figure 4 by W. Yang, *et al.*Figure 5 by W. Yang, *et al.*

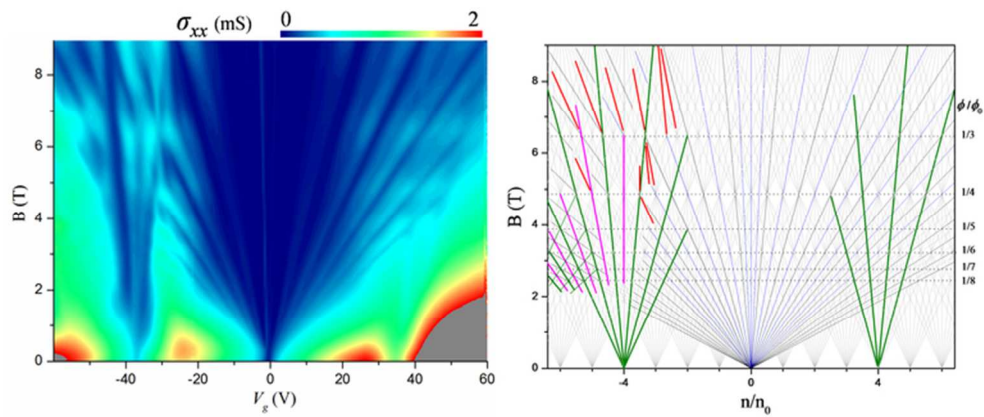


Table of Contents graphic  
33x13mm (600 x 600 DPI)