

Flows in one-dimensional and two-dimensional carbon nanochannels: Fast and curious

Mainak Majumder, Alessandro Siria, and Lydéric Bocquet

Carbon materials exist in a large number of allotropic forms and exhibit a wide range of physical and chemical properties. From the perspective of fluidics, particularly within the confines of the nanoscale afforded by one-dimensional carbon nanotubes (CNTs) and two-dimensional graphene structures, many unique properties have been discovered. However, other questions, such as the link between electronic states and hydrodynamics and accurate model predictions of transport, remain unanswered. Theoretical studies, experiments in large-scale ensembles of CNTs and stacked graphene sheets, and precise measurements at the single-pore and single-molecule level have helped in our understanding. These activities have led to explosive growth in the field, now known as carbon nanofluidics. The ability to produce membranes and devices from fluid phases of graphene oxide, which retain these special properties in molecular-scale flow channels, promises realization of applications in the near term.

Introduction

Carbon is a “go-to” material for applications in the fields of molecular separations via adsorption, as electrode materials in batteries, and for strong composite materials. From a fundamental point of view, carbon can form different types of hybridized bonds (sp , sp^2 , and sp^3), which underpin the formation of a wide variety of allotropes, including diamond, graphite, fullerenes, and nanotubes. Graphene, an individual carbon layer of monoatomic thickness, has also been isolated and its properties evaluated.

While wide-ranging experimental and theoretical work has been undertaken on the electronic, electrochemical, and mechanical properties of carbon allotropes, understanding and exploiting the molecular- and fluid-transport properties within the confines of the nanoscale afforded by the one-dimensional (1D) structure of carbon nanotubes (CNTs) and the two-dimensional (2D) planar structure of graphene is a new frontier. Carbon is special from the fluidic perspective, and the discovery of new nanofluidic behavior associated with graphitic materials has triggered explosive growth in this field. Much, however, remains to be discovered and understood. There is potential in these discoveries to lead to disruptive new technologies for water purification, desalination, and energy generation and storage. In this article, we focus primarily on experimental

studies of carbon nanostructures. Other articles in this issue review the theoretical studies undertaken in this field.

One-dimensional carbon channels

Molecular simulations have played a key role in the development of this field. In 2001, Hummer et al. investigated the water-conduction properties of single-walled CNTs and reported extraordinary water speeds in CNTs of around 90 cm s^{-1} under moderate pressure drops, comparable to aquaporin protein channels, an extremely performing biological water filter.¹ Around the same time, Johnson et al., using molecular dynamics (MD) simulations, reported orders of magnitude larger transport diffusivities of gases inside the smooth interiors of CNTs, compared to what was expected by classical hydrodynamics.² It was interesting to observe that two different states of matter—liquids and gases—with different molecular densities, showed similar behavior during flow through CNTs.

Several years later, experimental studies were undertaken when methods were developed to fabricate membranes composed of a large ensemble of vertically aligned CNTs. Carbon nanotubes were grown in a vertical array and the space between these tubes were filled with a polymer³ or ceramic.⁴ This consolidated film was released from the substrate to

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doi:10.1557/mrs.2017.62

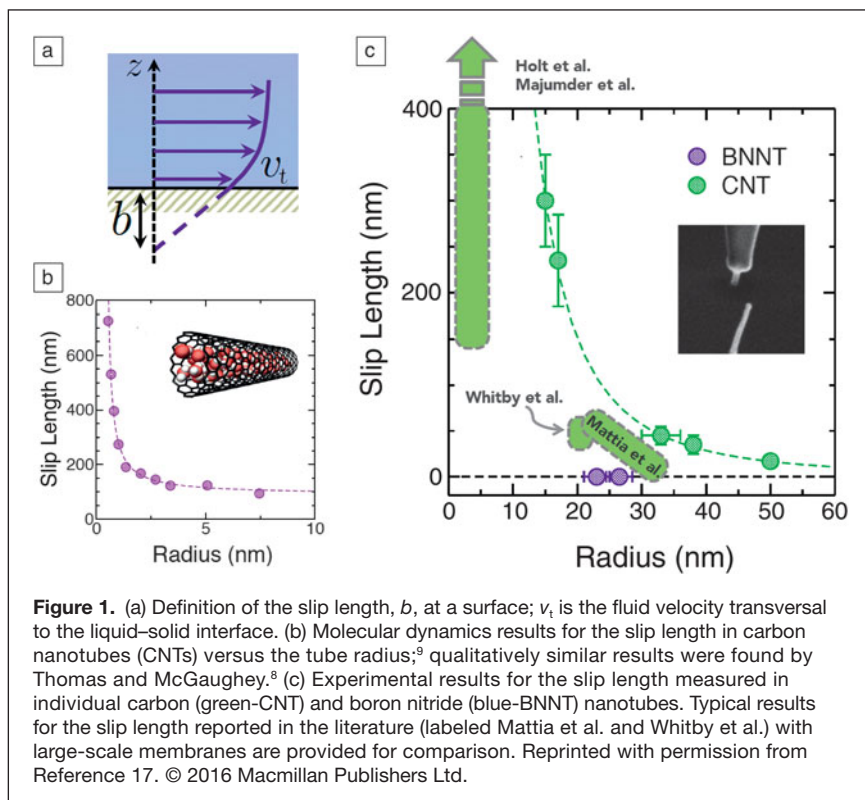
yield freestanding membranes. These studies demonstrated the ultrahigh permeability of CNT membranes, four to five orders of magnitude larger than standard continuum predictions for liquids and gases.^{4–6} However, there was some debate surrounding the origin of the superfast flows as well as the magnitude of the enhancements, because these measurements were averaged over a large number of nanotubes.⁷

Theoretical efforts for understanding the origins of enhanced flow in nanotubes confirmed a low wall-fluid friction coefficient at the water–nanotube surface as compared to other surfaces. Even more striking was that surface friction decreased with the radius of the CNT—smaller tubes lead to faster flows.^{8,9} As shown in **Figure 1**, surface friction of liquids is usually quantified in terms of a slip length, b , which accounts for the breakdown of the no-slip boundary condition at the CNT surface (a large slip length being associated with small friction).¹⁰ In the presence of surface slippage, the nanotube permeability, k_{NT} , defined in terms of the ratio between the averaged water velocity, v_w , and applied pressure drop, ΔP , is accordingly enhanced as:

$$v_w = \frac{k_{\text{NT}}}{\eta} \times \left(-\frac{\Delta P}{L} \right); \quad (1)$$

$$k_{\text{NT}} = \frac{R^2}{8} \left(1 + \frac{4b}{R} \right),$$

where R is the channel radius, L is the channel length, and η is the water viscosity.



Simulations report large slip in the hundreds of nanometers range, which increases when the CNT radius decreases.^{8,9} Values of slippage observed in CNTs are remarkable and exceed almost two orders of magnitude of that observed in any other material.¹⁰ This nanoscale behavior can be theoretically rationalized in terms of an increasing incommensurability of water with a crystalline CNT surface for smaller tubes.⁹

It has slowly and steadily emerged from the theoretical studies that CNTs are special for water conduction. To resolve this scientific question of enhanced fluid flow, increased experimental activity for single-pore measurements in CNTs has been reported. This has raised challenges in instrumentation, both in building well-defined individual nanofluidic channels amenable for a systematic fundamental understanding of their properties, as well as in measurements of minute ionic currents and water flows traversing these nanoscale pipes.

A number of groups have developed methods to isolate and embed single nanotubes into microscale chambers.^{11–13} Another approach consists of embedding CNTs directly into lipid bilayers and cell membranes, allowing the systematic study of ion and DNA translocation through such “CNT porins.”^{14,15} Siria et al. used nano-manipulation tools to insert a single nanotube into a pierced membrane, leading to a trans-membrane geometry that allows the exploration of ionic transport not only under electric fields, but also pressure drops and osmotic gradients.^{16–18} In most of these experiments, transport has been driven by electric fields, and the measured quantity is the ionic current traversing the individual channels, typically in the range of nanoamperes to picoamperes.

These studies demonstrate that ionic transport in CNTs is peculiar; for example, conductance scales sublinearly as a function of salt concentration.^{18,19} This can be rationalized in terms of ion adsorption at the carbon surface.¹⁸ Siria et al.¹⁶ also demonstrated giant, osmotically induced ionic currents in boron nitride nanotubes (BNNTs), the crystallographic cousin of CNTs. This property has been further confirmed in an alternative MoS_2 single-layer system;²⁰ it is now the object of technological transfer for the development of new membranes for the conversion of the energy coming from the mixing of solutions with different salinity, the so-called blue energy. We should also note that some of these experiments in CNTs have yielded results that are difficult to explain using standard theories of ionic transport, like the observation of blocking currents in single nanotubes.¹¹

Going from ionic to mass flow measurements is a further challenge in individual nanotubes. Secchi et al. were recently able to quantify the water flow across a single nanotube by harvesting the hydrodynamic peculiarity of nanojet flows.¹⁷ These experiments, the first to measure flow in

single nanotubes, have shown that considerable flow slippage occurs in CNTs and that the effect is enhanced in smaller diameter nanotubes (see Figure 1). Interestingly, these measurements raise new mysteries, as the slip increase is much larger than predicted by theory. The BNNTs exhibited no slip at all. It is worth noting that these two materials, which have the same crystallographic characteristics, but different electronic properties—boron nitride being strongly insulating in contrast to semimetallic carbon—exhibit different hydrodynamic behaviors. Recent explorations using *ab initio* simulation tools have shown that electronic degrees of freedom can strongly affect the physical chemistry and lead to considerable difference in transport properties.^{21,22}

To a large extent, the prediction of enhanced flow in nanotubes by simulations and experiments in both large-scale ensembles of CNTs and single-tube flow measurements should alleviate any doubt about the occurrence of superfast flows in CNTs. Despite this scientific assurance, vertically oriented CNT membranes are difficult to scale up, and after a decade of research, no product is currently available. It also remains to be seen if the fast fluid flow properties will lead to lower energy requirements for desalination, given that fast fluid flow would mean that the concentration polarization layers that would oppose the applied pressure would also increase rapidly.²³ Still, nanotubes remain a fascinating fundamental object, full of surprises.

Two-dimensional carbon channels

In terms of fluidics, driving forces scale with the inverse of the membrane thickness, so that molecularly thin membranes are associated with minimal flow resistance and maximal transport. Several research groups have used thin graphene layers grown by chemical vapor deposition, transferred it over a porous substrate, and utilized nanofabrication tools such as focused ion beam or focused ion beam-assisted chemical etching to develop permeable pores. This allows fabrication of porosities with tunable subnanometric pores sizes and large pore densities, up to 10^{12} cm^{-2} ,²⁴ making such membranes good candidates for molecular sieving applications (e.g., for desalination).²⁵ If no defects or holes are pierced, atomically thin 2D membranes made of graphene have been proven to be impermeable to all atoms and molecules at ambient pressure, making them the perfect support for developing new fluidics membranes. Interestingly, only protons seem to be able to permeate through defect-free graphene, with a slightly different result on h-BN.²⁶

As expected from their molecular thickness, such pierced membranes also demonstrated fast transport properties. Park et al.²⁷ verified that flow resistance is, however, limited by the hydrodynamic entrance effect—the lateral size of the nanopore, a , acts as a cutoff and the permeability in this case obeys the so-called Sampson Law, relating flux, Q , to the pressure drop ΔP (Figure 2):

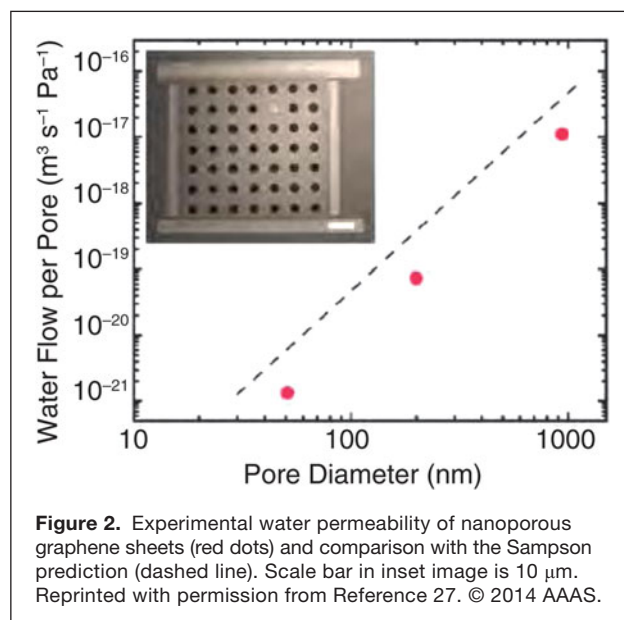
$$Q = \frac{a^3}{3\eta} \times (-\Delta P). \quad (2)$$

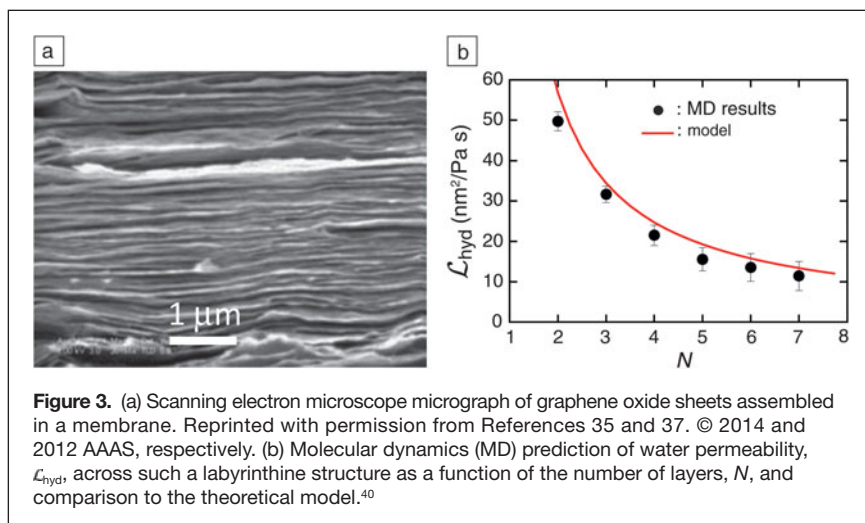
Geim and co-workers recently fabricated nanofluidic devices consisting of a few graphene layers as spacers between two

graphite surfaces and measured evaporation flows of water induced by capillarity across these channels.²⁸ They discovered the possibility of stacking graphene with controlled subnanometer confinement—this is the domain where “exotic” (non-classical) transport (and breakdown of bulk hydrodynamics) is expected. Geim et al. highlight the role of molecular disjoining pressure effects on transport leading to counterintuitive consequences, such as a higher flux for smaller confinements. In this regime, the Laplace expression for the capillary pressure breaks down and it depends on the number of water layers confined in the channels.²⁹ The ability to fabricate such nanofluidic systems allows for a new domain of fluid transport with the possibility of systematic fundamental exploration of their properties.

Molecular confinement can also be reached in larger-scale membranes, such as graphene oxide membranes composed of stacked carbon membranes, as in a layered French pastry called a “millefeuille” (see Figure 3). Graphite oxide (GO) shows rich colloidal behavior, including phase transitions from isotropic to liquid crystalline phases.^{30–32} Majumder and co-workers have recently developed methods to manufacture GO membranes in large scales compatible with roll-to-roll processing utilizing the liquid crystalline phases of GO.³³

The transport properties of such membranes composed of stacked layers of graphene oxide have been explored in various studies.^{34–38} In terms of flow, the characterization of the transport properties of these membranes has yielded contrasting results, with permeability results spanning orders of magnitude, so it is rather difficult to conclusively interpret the flow-enhancement mechanisms. There is thus a need to develop consistent materials characterization and measurement protocols.³⁹ However, due to its labyrinthine architecture, the hydrodynamic resistance of this structure is expected to be much larger than that of molecularly thin graphene, and





Future challenges to be addressed and conclusions

After more than a decade of intense investigations, both on the experimental and theoretical sides, the unique flow properties of carbon materials, which are far beyond expectations, have been confirmed. This period has seen the considerable development of carbon nanofluidics, which now offers the possibility of conducting single nanotube and single molecular channel experiments. This is a milestone, and opens new opportunities for the systematic exploration of transport properties of these systems.

These experiments have raised further mysteries, such as the strong contrast of flow properties inside semimetallic carbon structures versus the insulating boron nitride. This suggests that the interaction of water with the confining materials to a large extent remains to be understood, and a proper model is still needed to account for such effects. It is interesting to note that hydrodynamic properties depend so strongly on the electronic degrees of freedom. This suggests that carbon nanofluidics is an exciting fundamental playground where classical physics meets quantum physics, a research avenue that should be further explored.

Beyond fundamental questions, the specific properties of carbon materials still raise considerable hope for more applications. On the one hand, the fabrication challenges of large-scale CNT membranes has somewhat crushed the hope to use these 1D materials for separations and desalination applications at large scale. On the other hand, the development of 2D graphene materials and their stacked forms as graphene oxides now raises great hopes, because these materials retain many of the key advantages of carbon with a less prohibitive technical cost in terms of fabrication. In the end, the property to exploit may not be flow enhancement, but exploring their potential in a broader perspective for water transport and novel functionalities is definitely needed.

These new architectures have revived the hopes of harvesting carbon materials for industrial applications. This opens up new possibilities in membrane science. Industries need to invest and commercialize some of these novel fluidic platforms, which is only possible if high-value, high-volume applications are demonstrated and commercial potential unearthed.

In summary, the nascent field of carbon nanofluidics is at a crucial juncture of impact and growth because all the parts are accessible. The materials are readily available, the problems are laid out, and the experimental and theoretical tools have been developed.

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mainly controlled by (again) entrance effects between the various layers. This mechanism was rationalized theoretically in a recent report (Figure 3), and yielded good agreement with experimental results for liquid flows (provided experiments did not involve capillary menisci).⁴⁰

In terms of ionic transport, these stacked systems have demonstrated esoteric phenomena, such as ion-current rectification behavior depending on the shape of the membrane.⁴¹ Interpreting such results remains to be understood on the theoretical side, but they have potential in the construction of components of iontronic circuits, the ionic counterpart of electronic circuits.⁴²

Beyond these aspects, such stacked membranes may be advantageous for separations. Recent simulations have shown that GO membranes may exhibit a subtle “self-semipermeability” to water in the presence of ethanol, thereby opening the possibility of separating water from ethanol by a reverse osmosis-like process, which consumes considerably less energy than distillation processes.⁴³ GO membranes have been utilized for pervaporation, typically allowing water vapor to permeate through the membrane while retaining the organic components.⁴⁴ They have also demonstrated CO₂/N₂ selectivity depending upon the degree of interlocking of the GO sheets.³⁶ Importantly, both of these examples highlight molecular-scale separations.

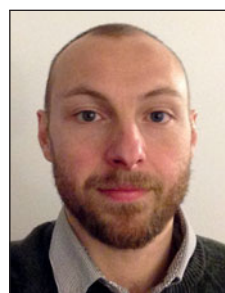
Another practical example is the use of GO membranes as a protective and permselective membrane on the sulfur cathode of Li-S batteries, enabling the transport of Li ions, but limiting the transport of the physically larger polysulfide species. The addition of the membrane in the battery architecture is found to dramatically increase the cyclability and transport kinetics in Li-S battery cells.⁴⁵ These membranes have also been reported to have better flux and selectivity performance than typical commercial nanofiltration polymeric membranes.³³ Their specific architecture, which is intrinsically molecular, combined with their ease of fabrication, offer great opportunities for membrane applications and a complex structure to model transport (see Figure 3b).⁴⁰

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