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Letter

A Klein-tunneling transistor with ballistic graphene

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Abstract

Today, the availability of high mobility graphene up to room temperature makes ballistic transport in nanodevices achievable. In particular, p-n-p transistors in the ballistic regime give access to Klein tunneling physics and allow the realization of devices exploiting the optics-like behavior of Dirac Fermions (DFs) as in the Veselago lens or the Fabry–Pérot cavity. Here we propose a Klein tunneling transistor based on the geometrical optics of DFs. We consider the case of a prismatic active region delimited by a triangular gate, where total internal reflection may occur, which leads to the tunable suppression of transistor transmission. We calculate the transmission and the current by means of scattering theory and the finite bias properties using non-equilibrium Green's function (NEGF) simulation.

Keywords: graphene, Klein tunneling, ballistic, transistor, Dirac fermion optics

1. Introduction

As a high mobility material, graphene is well suited to high frequency electronics [1, 2]. Additionally, thanks to the weakness of electron–phonon coupling [3–6], the high mobility persists at high temperature [7] so that one can envision ballistic graphene electronics in realistic operating conditions. The absence of a band-gap restricts the switching off capability of



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graphene, the conductivity reaching a shallow minimum at charge neutrality limited by the quantum of conductance $4e^2/h$. For logic electronic applications a band-gap can be restored using e.g. geometrical confinement [8], but this is usually at the cost of reduced mobility. In microwave electronics both a high mobility and a significant switching capability are needed to achieve large voltage and power gains at high frequency. To this end we explore here the new possibilities offered by Klein tunneling (KT), a hallmark of Dirac fermions (DFs).

We consider the case of p-n-p transistors where the resistance at the source–gate and gate–drain junctions is dominated by the *Klein tunneling effect*, while DFs propagate ballistically in the barrier [9]. With graphene being ambipolar, the generalization to n-p-n transistors is straightforward. This is the regime of DF optics where refraction and transmission at the interfaces are determined by Fresnel-like relations [10] and depend on the abruptness of junctions [11, 12]. Architectures exploiting the optical properties of DFs have been already proposed, such as the Veselago lens [11, 13], and demonstrated, such as Fabry–Pérot interferometers [14–16] or tilted p-n junctions [17, 18] (for a review, see reference [19]). The possibility of a ‘latticetronics’ of Klein tunneling currents in an armchair ribbon using potential barriers has also been recently discussed [20]. Here we consider a different geometry, that exploits total internal reflection in a *Klein tunneling prism*. The prism is made of an n-doped ballistic triangular domain embedded in a p-doped diffusive area, the latter being controlled electrostatically or chemically. As in light reflectors, an array of KT-prisms can be used to form the active channel of a *Klein tunneling transistor*; this geometry minimizes the gate length to keep ballistic transport conditions in a way similar to Fresnel lenses which minimize glass weight and light absorption [21]. In this work we calculate the low-energy transmission of such a device using scattering theory, i.e. within an intuitive and physically transparent approach. Our study is supplemented by atomistic simulations using the non-equilibrium Green’s function (NEGF) formalism that includes a more complete description of quantum transport. It gives access to finite bias properties while accounting for short gate effects like direct drain–source tunneling, diffraction, dispersion and finite temperature effects. Both approaches predict for the Klein tunneling transistor a strong suppression of conductance that can eventually go below the minimum conductance at charge neutrality. This transistor can be used as a tunable barrier for electrostatic quantum confinement to achieve, e.g. single Dirac fermion pumps working at low temperature. It is also suited for microwave electronics as it cumulates significant resistance in the OFF state with a large conductance in the ON state. A nanoscale variant has been recently proposed that predicts very large ON–OFF ratios for logic applications [22]. Our approach is different: it is based on geometrical DF optics following reference [23]; it is more conservative in accounting for diffusive transport in the leads and targets microwave electronic applications [24, 25].

The principle of the Klein tunneling prism is sketched in figure 1. It can be understood by scattering theory and relies on the total internal reflection in a triangular n-doped graphene region (concentration n , angle α), the refractive medium, embedded in a p-doped environment (concentration $p \lesssim n$) playing the role of vacuum. The refraction at the input p-n junction obeys a Snell–Descartes-like relation $\sin \phi_1 = \nu \sin \theta_1$ where $\nu = -\sqrt{n/p}$ is the (negative) refraction index [10] as sketched in the figure. The transmission $\mathcal{T}(\phi)$ can be calculated for a sharp junction [11], but also for smooth junctions (see below and reference [12]). The latter case is more realistic and suitable for device modeling. The main feature of Klein tunneling is the

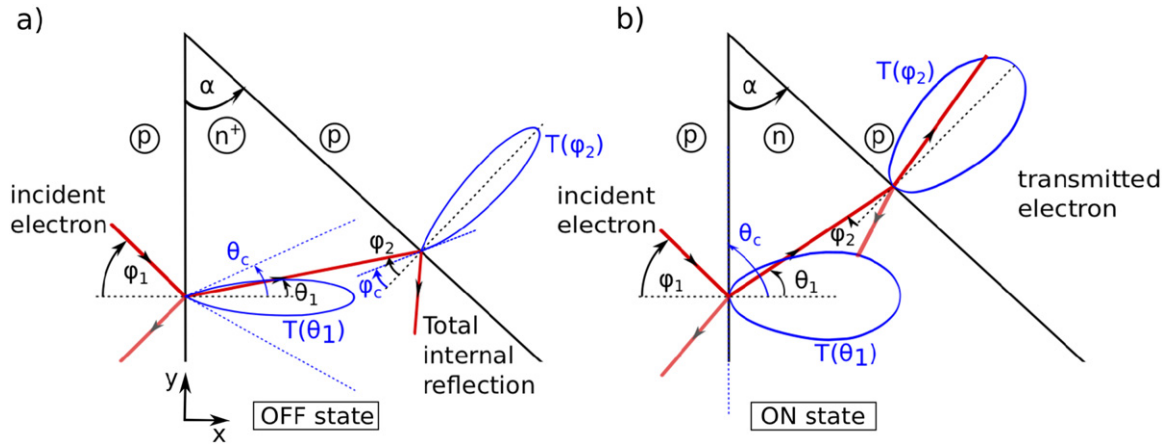


Figure 1. Principle of total reflection in a Klein tunneling prism. The refraction angle of Dirac fermion (DF) beams (red rays) and their angular dependent transmission amplitude (blue lobes) are controlled by the optical-like index ratio $\nu = -\sqrt{n/p}$ of the p and n regions. (a) OFF state $n \gg p$. Anisotropic forward scattering occurs at p-n junction: the refracted rays are mostly transmitted along the junction normal within a lobe limited by $|\theta_1| < \theta_c$. The n-p junction selects the incident carriers that are close to the normal to the junction (i.e. $|\phi_2| < \phi_c$); others being reflected. (b) ON state $n \simeq p$. In this case $\theta_c = \phi_c = 90$ deg which means all incident rays are transmitted with large transmission coefficients at both interfaces.

enhanced forward scattering for $n \gg p$. As shown in the figure, the refracted DF beam is focussed along the junction normal within an angular opening $|\theta_1| \leq \theta_c$, where $\theta_c = \arcsin(1/|\nu|)$ is the critical angle. At the drain side, which is an n-p junction where DFs are impinging at incidence $\phi_2 = \alpha - \theta_1$, the Snell–Descartes relation reads $\nu \sin \phi_2 = \sin \theta_2$. For $|\nu| \gg 1$, this implies total reflection for $|\phi_2| \geq \phi_c$, with $\phi_c = \theta_c$ for symmetric drain and source doping (and zero bias). The condition is met for any ray incident to the prism provided that $\theta_c < \alpha/2$ or $n > p / (\sin(\alpha/2))^2$. Finally, the reflected beams are transmitted back to the source junction. The reflection can be controlled and transmission restored, on decreasing n-doping, i.e. increasing θ_c , as shown in figure 1(b). Note that one obtains an equivalent effect on decreasing the prism angle down to $\alpha = 0$; it means that the transmission in the open state $n \simeq p$ (or $\nu = -1$) should approach that of a rectangular gate transistor. Taking $\alpha = 45$ deg, one can estimate the gate doping for full reflection: $n > 6.8p$ (or $|\nu| > 2.6$). The transmission of a KT transistor is suppressed here when increasing the gate doping deep in the metallic regime; this is a marked difference with conventional semiconducting transistors where transmission is suppressed on pinching-off the channel. Operating a transistor with a large intrinsic transmission should benefit the dynamical and noise properties of the device. In order to establish the above sketch, a full calculation is needed that accounts for finite transmission and multiple reflection effects.

We rely on the realistic modeling of the p-n junctions. Translational invariance along the junction parallel to the y-axis yields the above-mentioned Snell–Descartes relation between θ and

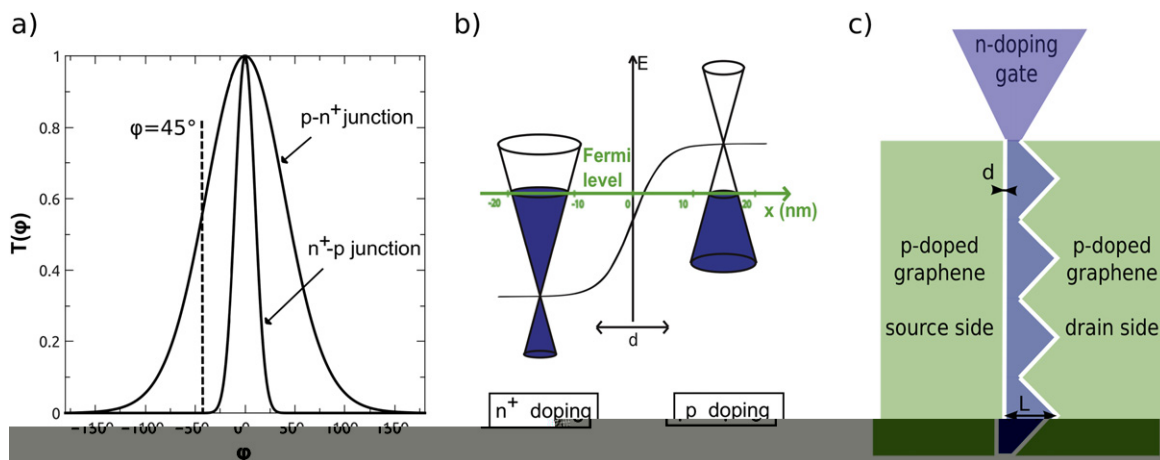


Figure 2. (a) Incident angle ϕ dependence of the transmission coefficient for smooth junction ($d = 10$ nm). Angular dependent transmission at a $p - n^+$ and a $n^+ - p$ junctions ($n^+ = 6p$); the contrast is most pronounced for an incidence angle $\phi = 45$ deg. (b) Sketch of the Fermi function potential profile and associated band structure of a $n^+ - p$ junction with the length of the junction $d = 10$ nm. (c) Sketch of a Klein tunneling transistor with its split gates. The barrier area is blue (n-doping gate) and the lead areas are green (p-doping gate). Here the Klein tunneling transistor is made of four elementary units.

ϕ . A smooth junction, characterized by a length $d \gg k_p^{-1}$ where k_p (resp. $k_n = |\nu|k_p$) is the Fermi wave number in p-doped (resp. n-doped) region, has a transmission $\mathcal{T}_{smooth}(\phi) \simeq \exp - \left[\pi d k_p^2 \sin^2 \phi / (k_p + k_n) \right]$ [11]. Dealing with intermediate junction length ($d \sim k_p^{-1}$), we rely on the expression by Cayssol *et al* reference [12], which is the exact solution for a potential step described by a Fermi function, $V(x) = V_0 (1 + \exp(-x/w))^{-1}$ (see figure 2(b)). We use $d = 4.5w$ to make contact with the smooth junction formula. The transmission is given by $\mathcal{T}(\phi) = 1 - \left[\sinh(\pi w k^{+-}) \sinh(\pi w k^{-+}) \right] / \left[\sinh(\pi w k^{++}) \sinh(\pi w k^{--}) \right]$, where $k^{a\beta} = k_p (1 + \alpha \cos \phi) + k_n (1 + \beta \cos \theta)$. The angular dependence $\mathcal{T}(\phi)$ is displayed in figure 2(a) for two representative configurations of the OFF state: $p-n^+$ and n^+-p junctions with $n^+ = 6p$. The contrast is most pronounced for $\phi \gtrsim 45$ deg with $T_{p-n^+} \lesssim 0.6$ and $T_{n^+-p} = 0$, which is the regime of total internal reflection. The contrast is close to that predicted for a sharp junction but different from that of a smooth junction (not shown) which justifies the use of the Cayssol interpolation formula.

The principle of the Klein tunneling prism can be realized in a Klein tunneling transistor (figure 2(c)) on stacking, head-to-tail, a series of prisms to realize a sawtooth gate with symmetric elementary units made of an isosceles triangle of opening angle $\pi - 2\alpha$. This geometry allows to implement the refractor principle while keeping the gate length short enough to remain in the ballistic regime. The n-doped barrier is assumed to be ballistic and controlled by the transistor gate. The leads can be either access regions or simply metallic contacts. In the latter case, the carrier concentration is set by electrochemical doping, in the former it

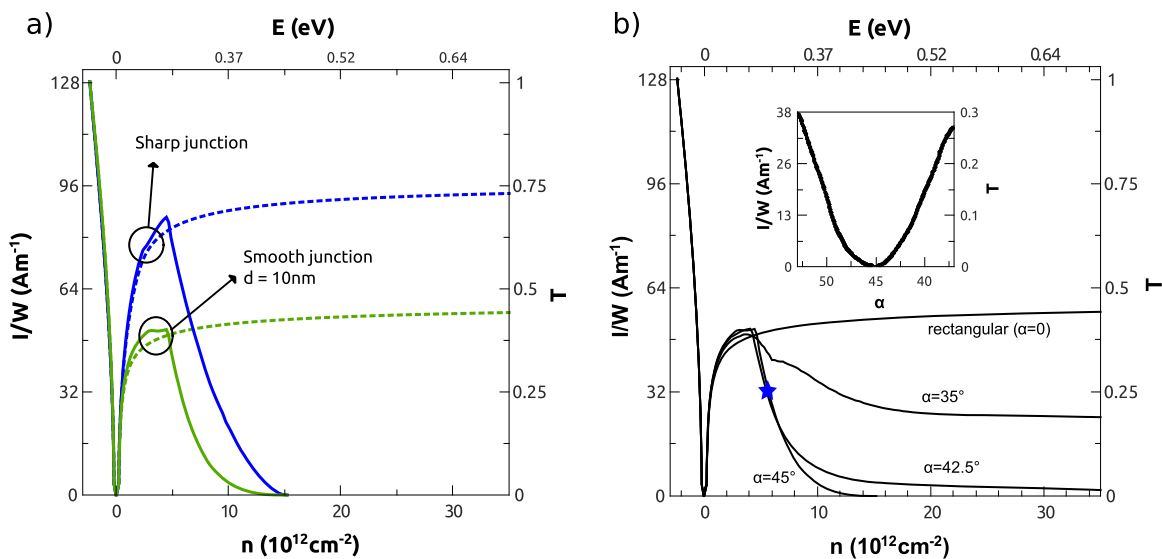


Figure 3. Current density I/W (and corresponding transmission T) from the scattering theory of various Klein tunneling p-n-p transistors as a function of gate doping n ; with lead doping of $p = 2.3 \times 10^{12}\text{cm}^{-2}$, for a rectangular gate (dotted lines in panel a) and saw-tooth gate (solid lines). The rectangular gate reproduces the well-known graphene transistor behaviour while the triangular geometry has its transmission suppressed at high doping. (a) Sharp junction (blue lines) shows a higher transmission than smooth junction (green lines) with a junction length of $d = 10\text{nm}$. (b) Transmission for various gate geometry from rectangular ($\alpha \rightarrow 0$) to $\alpha = 45^\circ$. Inset: α dependence of current density (and corresponding transmission) at $n = 6p$ with a minimum for the $\alpha = 45^\circ$ deg geometry. The star indicates the working point of a rf transistor.

can be tuned by a second electrostatic gate. To assess device properties, we calculate the transmission of DF rays across an elementary triangle. We consider a beam with a given incidence angle ϕ_1 and position y along the source side. The trajectory of the ray into the prism is calculated according to above p-n junction refraction and reflection rules iterated up to twenty internal reflections. The beam intensity inside the prism decreases at each reflection, the transmitted intensity outside the prism increases accordingly. We then integrate over y positions and all incident angles (diffusive leads) weighted by the angular density of states to get the overall transmission $T = \langle \mathcal{T} \rangle_{\phi,y}$. The results are plotted in figure 3 as function of gate doping, for $p = 2.3 \times 10^{12}\text{cm}^{-2}$. We estimate the current density per unit width W , $I/W = (4e^2/h)(k_p/\pi)TV_{ds}$, which is plotted here for a small $V_{ds} = 10\text{mV}$ bias. Panel (a) shows the effect of the junction sharpness for both rectangular and triangular gates; panel (b) shows that of the prism angle while keeping the gate area constant. In standard Klein tunneling with rectangular gates, the transmission saturates at 75% (resp. 45%) for sharp (resp. 10 nm-long) junctions which determines the ON-state current and conductance $g_{ON}/W \simeq 5\text{mS}\mu\text{m}^{-1}$ (10 nm-long junction). As seen in panel (b), the OFF-state current is very sensitive to the prism opening angle; it is zero for $\alpha = 45^\circ$ (and $n \gtrsim 6p$) but increases rapidly whenever α deviates by more than 5 deg from this value (see inset of figure 3(b)). From this analysis, we conclude that the optimal geometry for a KT transistor is $\alpha = 45 \pm 5^\circ$ and

abrupt junctions ($d \lesssim 10$ nm). This estimate is characteristic of the robustness of the device against geometrical imperfections, like prism asymmetry, apex rounding or p-n junction roughness. In these conditions, one obtains a significant modulation of transmission in the range 0–0.4 which is appropriate for electrostatic confinement in quantum dots. From the slope of the $I(V_{ds})$ curve (working point labeled by a star in figure 3(b)) and considering a gate capacitance $c_g = 10$ fF μm^{-2} (equivalent SiO₂ thickness of 3 nm), we estimate the bias dependence of transconductance per unit width $g_m V_{ds}^{-1}/W \simeq 8$ mS $\mu\text{m}^{-1}\text{V}^{-1}$, of voltage gain $A_V V_{ds} = A_V V_{ds}^{-1} = g_m V_{ds}^{-1}/g_{ds} \gtrsim 3$ V⁻¹ and of transit frequency $f_T/V_{ds} = g_m/(2\pi c_g L W V_{ds}) \simeq 1300$ GHz V⁻¹ (for a gate length $L = 100$ nm).

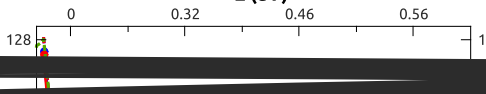
We discuss now the physical limits of our geometrical optics description which relies on the assumption that $d \lesssim k_p^{-1} \ll L$. The refraction principle is scale independent but in practice the characteristic length of the gate L should be smaller than the ballistic length, while remaining larger than the electronic wave length to avoid deleterious effects of diffraction. The principle of the reflector being very sensitive to refraction angles (see the inset of figure 2), an uncertainty $\Delta\theta \sim (k_p L)^{-1}$ in angular orientation, due to finite wavelength, may drastically affect the total internal reflection. Another limitation for the OFF state resistance is the direct drain source tunneling which is also strongly scale dependent. Finally we have neglected for simplicity the dispersion effects arising from broad sources such as finite bias DF emission. In order to quantify these effects we have performed a numerical simulation of the KT transistor by means of NEGF method. Our model is based on a tight-binding Hamiltonian to describe the electron state in the graphene honeycomb lattice [26].

NEGF simulation assumes a transistor of ballistic graphene whose size is scaled down by a factor 2.5 with respect to a realistic device to make the calculation achievable with available computational resources. Additionally, the self-consistent solution of Poisson's equation has been deactivated here to save CPU time. The gate-induced potential in graphene was modelled as a 'square' barrier of height reduced by $V_{ds}/2$ at the source-end and enhanced by $V_{ds}/2$ at the drain-end. This simple description of potential has been shown realistic from self-consistent simulation of usual graphene field effect transistors (GFETs) in the p-n-p or n-p-n regimes [27]. The transistor gate is taken either as rectangular or triangular but with the same gate area. The triangular gate is an elementary unit of figure 2(c). The channel width is 80 nm; the gate length is 40 nm for the rectangular device. It is modulated between 20 nm and 60 nm for the triangular device. We set the source side doping to $p = 2.3 \times 10^{12}$ cm⁻² which corresponds to a Fermi energy $E_F = \hbar v_F \sqrt{\pi p} \simeq 0.15$ eV. The NEGF simulation provides the transmission coefficient $T(\varepsilon)$ through the device, where ε is the carrier energy, considering the charge neutrality point (CNP) of the source as the zero energy reference. Two situations are considered: a low bias case $V_{ds} = 10$ mV $\ll E_F/e$ (figures 4(a) and 5(a)) and high bias case $V_{ds} = 200$ mV $\gtrsim E_F/e$ (figures 4(b) and 5(b)). The former allows direct comparison with (zero bias) scattering calculations; the latter is typical of a transistor working point.

In figure 4 $T(\varepsilon)$ is displayed for the rectangular geometry (red lines) and the triangular geometry (blue lines) for the ON state of the transistor (dotted lines) and the OFF state (solid lines). In the ON state (small gate doping) two minima of transmission appear corresponding to the energy position of the CNP in the lead and in the barrier. A transmission maximum is

a)

$V_{ds} = 10\text{mV}$
 $E \text{ (eV)}$



b)

$V_{ds} = 200\text{mV}$

actual devices and to evaluate their potential in terms of single electron pumps and microwave electronics.

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