Hot Electron Cooling by Acoustic Phonons in Graphene


1Laboratoire Pierre Aigrain, ENS-CNRS UMR 8551, Université P. et M. Curie and Paris-Diderot, 24, rue Lhomond, 75231 Paris Cedex 05, France
2Laboratoire de Photonique et Nanostructures, CNRS-UFR20 CNRS, Route de Nozay, 91460 Marcoussis Cedex, France

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We have investigated the energy loss of hot electrons in metallic graphene by means of GHz noise thermometry at liquid helium temperature. We observe the electronic temperature \( T \propto V \) at low bias in agreement with the heat diffusion to the leads described by the Wiedemann-Franz law. We report on \( T \propto \sqrt{V} \) behavior at high bias, which corresponds to a \( T^4 \) dependence of the cooling power. This is the signature of a 2D acoustic phonon cooling mechanism. From a heat equation analysis of the two regimes we extract accurate values of the electron-acoustic phonon coupling constant \( \Sigma \) in monolayer graphene. Our measurements point to an important effect of lattice disorder in the reduction of \( \Sigma \), not yet considered by theory. Moreover, our study provides a strong and firm support to the rising field of graphene bolometric detectors.

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Many remarkable properties of graphene stem from the chiral Dirac-fermion nature of carriers and the associated semimetallic density of states [1,2]. Graphene is also peculiar from the phonon point of view with a large optical phonon (OP) energy of 160–200 meV and a weak coupling of electrons to acoustic phonons (APs) [3–6]. The latter is due to the nonionic character of the lattice and the 2D nature of the phonons. Both effects conspire to the weak electron-phonon scattering responsible for the high intrinsic carrier mobility of graphene up to room temperature [7]. The OP scattering reappears, however, in the high-field transport, where OP emission by energetic electrons gives rise to current saturation [8,9]. By contrast, extrinsic disorder effects usually obscure AP scattering which remains thus more elusive and still debated [10]. The AP coupling becomes, however, prominent in heat transport as it constitutes the bottleneck in the cooling process of hot electrons to the substrate. Heat transport experiments in graphene offer thus the possibility to characterize electron-AP coupling in detail. On the application side, the weak AP coupling opens an avenue for the realization of fast and sensitive bolometric detectors working in a broad frequency spectrum ranging from microwave to optics [11–15]. Also in this respect an in-depth and direct characterization of hot-electron effects will prove useful.

In this Letter we report on the interaction between electrons and acoustic phonons in monolayer graphene. To this end, we have investigated the bias dependence of the electron temperature deduced from radio frequency shot noise measurements. Our experiment provides a direct access to the electron-phonon coupling constant. We rely on the relation \( S_I = 4k_BT_e/R \) between the current noise spectrum \( S_I \), the average electronic temperature \( T_e \), and the sample resistance \( R \). Johnson-noise thermometry has proven useful to study carbon nanotubes [16–18] and more recently graphene nanoribbons [19] and bilayer-graphene [20]. From an experimental point of view, we measure noise in the MHz to GHz band to overcome the environmental \( 1/f \) contribution while keeping quasi-stationary response conditions [21]. At sufficiently high bias, we find \( T_e \propto \sqrt{V} \), where \( V \) is the applied voltage. This is a signature of 2D acoustic phonons. We observe it in diffusive samples where the \( I-V \) characteristics are linear and optical phonon scattering is absent. At low bias we recover the \( T_e \propto V \) behavior, expected for heat conduction to the contacts, and described by the Wiedemann-Franz law. Both regimes are well explained by the heat equation. By fitting it to our measurements we extract the coupling constant \( \Sigma \) as a function of carrier density for samples on different substrates.

We present data of three representative devices: two large exfoliated graphene flakes deposited on hexagonal boron nitride (hBN) and a smaller sample on SiO\(_2\) made from chemical vapor deposition (CVD) graphene. The samples, labeled BN1, BN2, and CVD1, respectively, are sketched in Fig. 1. Samples BN1 and BN2 consist of a stack of a monolayer graphene and a 30 nm-thick hBN platelet on a Si/SiO\(_2\) substrate. The hBN platelet of approximately 10 \( \mu \text{m} \) diameter was produced by exfoliation of a high quality hBN powder (St. Gobain “Très BN”). The graphene flake was also obtained by exfoliation and placed on top of the hBN using a wet transfer technique [22]. CVD1 was made from a graphene sheet grown on copper, transferred to the Si/SiO\(_2\) [23]. The samples were produced by means of \( e \)-beam lithography and dry etching. Doped silicon was used as a back gate, with a 1 \( \mu \text{m} \) thick oxide, and each sample was embedded in a coplanar waveguide adapted for GHz frequencies [24]. Palladium...
metallizations ensure low Ohmic contacts to graphene. Table I lists the samples’ dimensions and electrical characteristics.

Measurements were carried out in liquid helium at 4.2 K to ensure a cold phonon bath. The amplification line, of bandwidth 0.8 GHz, is similar to the one in Ref. [16]. It includes a cryogenic low-noise amplifier (amplifier noise temperature of 8 K), calibrated against the Poissonian noise of a 460 Ohms $\text{Al}_x\text{AlO}_y\text{Al}$ tunnel junction. The samples’ $I-V$ characteristics were measured via the voltage drop across the bias resistance. In situ current annealing was performed to improve the samples’ electrical characteristics. The carrier density $n_s$ of samples BN1 and BN2 is deduced from the gate dependence of the dc conductivity in a range of $V_g = \pm 18 \text{ V(BN1)}$ and $V_g = \pm 28 \text{ V(BN2)}$. Sample BN1 stayed $p$ doped over the whole gate range whereas BN2 could be swept through the neutrality point. Sample mobility is estimated from the gate voltage dependence of the conductivity $\mu = 1/C_g \partial \sigma/\partial V_g$ with $C_g = 35 \text{ aF}\mu\text{m}^{-2}$. BN2’s mobility is on the order of $3000 \text{ cm}^2\text{ V}^{-1}\text{ s}^{-1}$, about a factor 10 larger than that of BN1. The conductance of CVD1 was independent of $V_g$ which indicates a highly doped regime; we estimate the carrier concentration on the order of a few $10^{13} \text{ cm}^{-2}$ from Hall-bar measurements on similar CVD sheets.

We turn now to the presentation of measurements. Figure 2(a) shows typical current noise spectra for different bias voltages. At low bias the spectrum is flat, whereas at higher bias a $1/f$ contribution clearly arises. Our broad-band setup allows us to quantitatively separate the white shot noise contribution $S_I$ from $1/f$ noise by fitting the spectra with a $S_I + C/f$ law. We find $C \propto I^2$ in accordance with the Hooge law [25]. This procedure is especially important for small samples where the $1/f$ contribution is larger. Figures 2(b) and 2(c) show the current $I$ and the shot noise $S_I$ of sample BN1 as a function of bias for three gate voltages. We restrict our study to biases where the $I-V$ characteristics are linear as the lack of current saturation is an indication of the absence of optical phonon scattering [8]. This is consistent with a transport scattering length ($\sim 10 \text{ nm}$) much smaller than the optical phonon scattering length ($\sim 200 \text{ nm}$) [8]. The shot noise is strongly sub-linear with respect to bias voltage and depends on gate voltage, with larger noise at higher carrier concentration. We extract the bias dependence of the average electronic temperature $T_e(V) = S_I R/4k_B$ from the measured shot noise. The results for sample BN1 at five gate voltages are displayed in Fig. 3. The electronic temperature

![FIG. 1 (color). Shot noise measurement scheme with a sketch of the sample the electrical environment. The bias resistance is $R_{\text{bias}} = 4732 \Omega$. The samples and the cryogenic low-noise amplifier are cooled at 4.2 K. The scanning electron microscope pictures refer to samples BN1 and CVD1: BN1 consists of an exfoliated graphene flake (red), deposited on an exfoliated hBN platelet (green), itself deposited on a Si/SiO$_2$ used as a back gate. CVD1 was fabricated from CVD grown graphene deposited on Si/SiO$_2$. Both samples are contacted with Pd electrodes (yellow).](image-url)
increases with bias voltage and reaches several hundred Kelvin at high bias. This value is well above bath temperature but still below the optical phonon energy of $\approx 200$ meV. We find that $T_e$ is weakly dependent on gate voltage and the different curves closely follow the $T_e \propto \sqrt{V}$ law (solid line) predicted for 2D acoustic phonons. A $T_e \propto V^{2/5}$ dependence (gray dashed line) is also plotted in the figure to highlight the different behavior expected for a $T^5$ law characteristic of 3D acoustic phonon cooling. Deviations are, however, observed at low bias where data rather follow a $T_e \propto V$ law. At the low end of the investigated bias range, the quasiequilibrium approximation required to define an electron temperature may fail due to large electron-electron scattering lengths [26,27]. From a Fano factor analysis, we estimate this mesoscopic regime to arise below a few tens of mV [28].

The electron temperature is determined by the balance between the Joule heating and the cooling powers at play [29]. Joule heating per unit area is $P = V^2/RLW$, while cooling is provided by two mechanisms: the first is electron heat diffusion to the leads, the second electron-AP interactions. At sufficiently high bias the diffusive contribution can be neglected; i.e., the cooling power is given by $\Sigma(T_e^4 - T_{ph}^4)$, where $T_{ph}$ is the phonon temperature. In graphene $\delta = 4$ has been proposed to account for the purely two dimensional APs [4,6]. In general $\delta$ varies from 3 to 6 [30]; the lower value $\delta = 3$ is observed in 1D systems such as carbon nanotubes [18] and $\delta = 5$ is typically used for 3D metals [26,31]. For a quantitative analysis of our data, we solve the heat equation

$$\frac{L \partial^2 T^2}{2R \partial x^2} = -\frac{V^2}{R} + LW \Sigma [T^4(x) - T_{ph,b}^4].$$

where $L = \pi^2 k_B^2/3e^2$ is the Lorenz number and $x$ denotes the coordinate along the graphene channel. We obtain an analytical solution in the case of cold contacts and cold phonon bath ($T_{ph} = 0$). The solution depends on a single free parameter $\Sigma$, which sets the two characteristic scales of the system: the temperature $T_S = (V^2/RLW \Sigma)^{1/4}$ and the voltage $V_S = L/(\sqrt{4RLW} \Sigma)$. $T_S = (P/\Sigma)^{1/4}$ is the maximum temperature reached in the absence of electron heat conduction, whereas $V_S$ defines the crossover voltage between the electron cooling at low voltages and phonon cooling regime at high bias. The temperature profile is pseudoparabolic at low bias [29] and evolves toward a uniform temperature $T(x) = T_S$ at high bias. The spatial average $T_e = \langle T(x) \rangle$ is then calculated numerically.

In Fig. 4 we plot the temperature data in the form $T_e^2/P$ as a function of $V$ with the corresponding error bars. Because of a more pronounced $1/f$ contribution, the error increases with increasing bias. The $T_e^2/P$ representation allows for a better comparison with theory and puts the emphasis on the density dependence of $\Sigma$. The plateaus at high bias and the dips at low bias reflect the $T_e \propto \sqrt{V}$ and $T_e \propto V$ regimes observed in the shot noise data (Fig. 3). The measurements are well fitted by the solution of Eq. (1) taking $\Sigma$ as the only free parameter (solid lines). We find $\Sigma \approx 2$ mW/m$^2$K$^4$ and a clear dependence on carrier density in BN samples, and $\Sigma \approx 0.42$ mW/m$^2$K$^4$ in CVD1. Since the dip at low bias marks the effect of electron heat diffusion to the leads, the crossover is more pronounced in the shorter CVD1 sample. This can be seen in Fig. 4(a) where the width of the dip is larger and agreement between data and theory is more quantitative. The fact that theory, with a single free parameter, accounts for both the plateau and the dip is a strong confirmation of the model and the underlying 2D acoustic phonon
mechanism. A small negative slope is observed at high bias; it may arise from the onset of an additional cooling mechanism due to electron coupling with either optical phonons or substrate phonons. However, due to limited experimental resolution at high bias, a separate study will be necessary to make a definitive conclusion about such a correction. Figure 4(c) shows the carrier-density dependence $\Sigma(n_s)$ and emphasizes its sensitivity to carrier mobility and disorder. This observation is consistent with the smaller values of $\Sigma$ in the CVD1 sample.

The aforementioned $\Sigma T^4$ law for electron-AP cooling is similar to a $\Sigma_k T^4$ law for phonon black body radiation to the substrate or the bath ($T_0$). This mechanism would occur in a hot phonon regime where $T_{ph} \approx T_e \gg T_0$. However, the corresponding coupling constant $\Sigma_k$ is about 3–4 orders of magnitude larger than $\Sigma$ measured in our experiments [32, 33]. Both mechanisms appear in series in the electron cooling process, thus giving rise to an effective coupling $\tilde{\Sigma} = \Sigma \Sigma_k / (\Sigma + \Sigma_k) \approx \Sigma$. This justifies our earlier hypothesis $T_{ph}^4 \ll T_e^4$ in Eq. (1).

We now come to the discussion of the results. According to theory [4, 6], longitudinal acoustic phonons (LA) are coupled to electrons via the deformation potential $D$ (10–30 eV). Theory predicts a cooling power $P = \Sigma_L A T^4$ with $\Sigma_L A \propto D^2 \sqrt{n_e}$ in the nondegenerate metallic regime and a different $P(T)$ law at high temperature. Taking $D = 10$ eV, this gives $\Sigma_L A \approx 10 \sqrt{n_e} / 10^{12} \text{mW/m}^2 \text{K}^4$. Our experiment confirms the $P = \Sigma T^4$ dependence in the metallic regime, but we find a smaller coupling constant, $\Sigma = 0.5 \text{mW/m}^2 \text{K}^4$ for BN1 and $\Sigma = 2 \text{mW/m}^2 \text{K}^4$ for BN2 at $n_s = 10^{12} \text{cm}^{-2}$. The discrepancy in $\Sigma$ cannot be explained by experimental uncertainties. Our experiment suggest the effect of lattice disorder, which is the limiting factor for the mobility, as a possible cause of the reduction of the electron-phonon coupling. As a matter of fact, lattice disorder, which is known to affect phonon lifetime [32],
and possibly also the phonon density of states, is not taken into account by theory for the metallic regime [4,6]. In the high-temperature regime however, a recent theory shows that disorder mediated phonon-phonon collisions may be important [36].

In conclusion, we have studied the interaction between electrons and acoustic phonons in diffusive graphene by measuring the energy loss of hot electrons. We find that the cooling power due to acoustic phonons follows a $2T^4$ law. We find that $\xi$ increases with carrier concentration, but the value, $\xi \approx 2$ mW/m²/K⁴, is approximately 1 order of magnitude smaller than predictions for LA phonons. Our work is a motivation for further theoretical investigation that takes into account the role of lattice disorder on phonons. Besides its implication for electron-phonon physics, our study of thermal noise is of direct relevance for the performance of graphene detectors.

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*bernard.placais@lpa.ens.fr

Present address: Laboratoire de Photonique et Nanostructures, 91460 Macoussis Cedex, France.


[28] In our samples, the Fano factor extrapolates to a value close to 1/3 at vanishing voltage.


[33] F. Pobell, Matter and Methods at Low Temperatures (Springer-Verlag, Berlin, 2007), 3rd ed., Fig. 4.5, p. 103.

